Chapter Thirteen KINETIC THEORY

MCQ I

- **13.1** A cubic vessel (with faces horizontal + vertical) contains an ideal gas at NTP. The vessel is being carried by a rocket which is moving at a speed of 500m s⁻¹ in vertical direction. The pressure of the gas inside the vessel as observed by us on the ground
 - (a) remains the same because 500m s^{-1} is very much smaller than v_{rms} of the gas.
 - (b) remains the same because motion of the vessel as a whole does not affect the relative motion of the gas molecules and the walls.
 - (c) will increase by a factor equal to $(v_{rms}^2 + (500)^2) / v_{rms}^2$ where v_{rms} was the original mean square velocity of the gas.
 - (d) will be different on the top wall and bottom wall of the vessel.
- **13.2** 1 mole of an ideal gas is contained in a cubical volume *V*, ABCDEFGH at 300 K (Fig. 13.1). One face of the cube (EFGH) is made up of a material which totally absorbs any gas molecule

incident on it. At any given time,

- (a) the pressure on EFGH would be zero.
- (b) the pressure on all the faces will the equal.
- (c) the pressure of EFGH would be double the pressure on ABCD.
- (d) the pressure on EFGH would be half that on ABCD.
- **13.3** Boyle's law is applicable for an
 - (a) adiabatic process.
 - (b) isothermal process.
 - (c) isobaric process.
 - (d) isochoric process.
- **13.4** A cylinder containing an ideal gas is in vertical position and has a piston of mass *M* that is able to move up or down without friction (Fig. 13.2). If the temperature is increased,



- (a) both *p* and *V* of the gas will change.
- (b) only *p* will increase according to Charle's law.
- (c) *V* will change but not *p*.
- (d) p will change but not V.
- **13.5** Volume versus temperature graphs for a given mass of an ideal gas are shown in Fig. 13.3 at two different values of constant pressure. What can be inferred about relation between $P_1 \& P_2$?
 - (a) $P_1 > P_2$
 - (b) $P_1 = P_2$
 - (c) $P_1 < P_2$
 - (d) data is insufficient.







В

Fig. 13.1

Exemplar Problems-Physics

- **13.6** 1 mole of H_2 gas is contained in a box of volume $V = 1.00 \text{ m}^3$ at T = 300 K. The gas is heated to a temperature of T = 3000 K and the gas gets converted to a gas of hydrogen atoms. The final pressure would be (considering all gases to be ideal)
 - (a) same as the pressure initially.
 - (b) 2 times the pressure initially.
 - (c) 10 times the pressure initially.
 - (d) 20 times the pressure initially.
- **13.7** A vessel of volume *V* contains a mixture of 1 mole of Hydrogen and 1 mole of Oxygen (both considered as ideal). Let $f_1(v)dv$, denote the fraction of molecules with speed between *v* and (v + dv) with $f_2(v)dv$, similarly for oxygen. Then
 - (a) $f_1(v) + f_2(v) = f(v)$ obeys the Maxwell's distribution law.
 - (b) $f_1(v), f_2(v)$ will obey the Maxwell's distribution law separately.
 - (c) Neither $f_1(v)$, nor $f_2(v)$ will obey the Maxwell's distribution law.
 - (d) $f_2(v)$ and $f_1(v)$ will be the same.
- **13.8** An inflated rubber balloon contains one mole of an ideal gas, has a pressure *p*, volume *V* and temperature *T*. If the temperature rises to 1.1 *T*, and the volume is increaset to 1.05 V, the final pressure will be
 - (a) 1.1 p
 - (b) p
 - (c) less than p
 - (d) between *p* and 1.1.

MCQ II



Fig. 13.4

13.9 ABCDEFGH is a hollow cube made of an insulator (Fig. 13.4). Face ABCD has positve charge on it. Inside the cube, we have ionized hydrogen.

The usual kinetic theory expression for pressure

- (a) will be valid.
- (b) will not be valid since the ions would experience forces other than due to collisions with the walls.
- (c) will not be valid since collisions with walls would not be elastic.
- (d) will not be valid because isotropy is lost.

13.10 Diatomic molecules like hydrogen have energies due to both translational as well as rotational motion. From the equation in

kinetic theory
$$pV = \frac{2}{3}E$$
, E is

- (a) the total energy per unit volume.
- (b) only the translational part of energy because rotational energy is very small compared to the translational energy.
- (c) only the translational part of the energy because during collisions with the wall pressure relates to change in linear momentum.
- (d) the translational part of the energy because rotational energies of molecules can be of either sign and its average over all the molecules is zero.
- **13.11** In a diatomic molecule, the rotational energy at a given temperature
 - (a) obeys Maxwell's distribution.
 - (b) have the same value for all molecules.
 - (c) equals the translational kinetic energy for each molecule.
 - (d) is (2/3)rd the translational kinetic energy for each molecule.
- **13.12** Which of the following diagrams (Fig. 13.5) depicts ideal gas behaviour?



- **13.13** When an ideal gas is compressed adiabatically, its temperature rises: the molecules on the average have more kinetic energy than before. The kinetic energy increases,
 - (a) because of collisions with moving parts of the wall only.
 - (b) because of collisions with the entire wall.

- (c) because the molecules gets accelerated in their motion inside the volume.
- (d) because of redistribution of energy amongst the molecules.

VSA

- **13.14** Calculate the number of atoms in 39.4 g gold. Molar mass of gold is 197g mole⁻¹.
- **13.15** The volume of a given mass of a gas at 27°C, 1 atm is 100 cc. What will be its volume at 327°C?
- **13.16** The molecules of a given mass of a gas have root mean square speeds of $100 \,\mathrm{m\,s^{-1}}$ at 27°C and 1.00 atmospheric pressure. What will be the root mean square speeds of the molecules of the gas at 127°C and 2.0 atmospheric pressure?
- **13.17** Two molecules of a gas have speeds of $9 \times 10^6 \text{ m s}^{-1}$ and $1 \times 10^6 \text{ m s}^{-1}$, respectively. What is the root mean square speed of these molecules.
- **13.18** A gas mixture consists of 2.0 moles of oxygen and 4.0 moles of neon at temperature *T*. Neglecting all vibrational modes, calculate the total internal energy of the system. (Oxygen has two rotational modes.)
- **13.19** Calculate the ratio of the mean free paths of the molecules of two gases having molecular diameters 1 A and 2 A. The gases may be considered under identical conditions of temperature, pressure

SA

and volume.

13.20 The container shown in Fig. 13.6 has two chambers, separated by a partition, of volumes $V_1 = 2.0$ litre and $V_2 = 3.0$ litre. The chambers contain $\mu_1 = 4.0$ and $\mu_2 = 5.0$ moles of a gas at pressures $p_1 = 1.00$ atm and $p_2 = 2.00$ atm. Calculate the pressure after the partition is removed and the mixture attains equilibrium.

13.21 A gas mixture consists of molecules of types A, B and C with masses $m_A > m_B > m_C$. Rank the three types of molecules in decreasing order of (a) average K.E., (b) rms speeds.



Fig 13.6

13.22 We have 0.5 g of hydrogen gas in a cubic chamber of size 3cm kept at NTP. The gas in the chamber is compressed keeping the temperature constant till a final pressure of 100 atm. Is one justified in assuming the ideal gas law, in the final state?

(Hydrogen molecules can be consider as spheres of radius 1 ${\rm \AA}$).

- **13.23** When air is pumped into a cycle tyre the volume and pressure of the air in the tyre both are increased. What about Boyle's law in this case?
- **13.24** A ballon has 5.0 g mole of helium at 7°C. Calculate
 - (a) the number of atoms of helium in the balloon,
 - (b) the total internal energy of the system.
- **13.25** Calculate the number of degrees of freedom of molecules of hydrogen in 1 cc of hydrogen gas at NTP.
- **13.26** An insulated container containing monoatomic gas of molar mass m is moving with a velocity v_o . If the container is suddenly stopped, find the change in temperature.

LA

- 13.27 Explain why
 - (a) there is no atmosphere on moon.
 - (b) there is fall in temperature with altitude.
- **13.28** Consider an ideal gas with following distribution of speeds.



- (i) Calculate V_{rms} and hence T. ($m = 3.0 \times 10^{-26}$ kg)
- (ii) If all the molecules with speed 1000 m/s escape from the system, calculate new V_{rms} and hence T.

Exemplar Problems-Physics

- **13.29** Ten small planes are flying at a speed of 150 km/h in total darkness in an air space that is $20 \times 20 \times 1.5$ km³ in volume. You are in one of the planes, flying at random within this space with no way of knowing where the other planes are. On the average about how long a time will elapse between near collision with your plane. Assume for this rough computation that a saftey region around the plane can be approximated by a sphere of radius 10m.
- **13.30** A box of $1.00m^3$ is filled with nitrogen at 1.50 atm at 300K. The box has a hole of an area 0.010 mm^2 . How much time is required for the pressure to reduce by 0.10 atm, if the pressure outside is 1 atm.
- **13.31** Consider a rectangular block of wood moving with a velocity v_0 in a gas at temperature *T* and mass density ρ . Assume the velocity is along *x*-axis and the area of cross-section of the block perpendicular to v_0 is *A*. Show that the drag force on the block is

 $4\rho A v_0 \sqrt{\frac{kT}{m}}$, where *m* is the mass of the gas molecule.