

NORTH EX PUBLIC SCHOOL
(Senior Secondary, Affiliated to CBSE)
(School block, Jain Nagar Sector-38, Rohini, Delhi-81)

CLASS-IX
SUBJECT-MATHS
CHAPTER-1 NUMBER SYSTEM

TOPICS/ INTRODUCTION:

1. Natural Numbers: Numbers from 0 (zero) onward are known as Natural numbers, denoted by 'N'.
 $N = \{1, 2, 3, 4, \dots\}$
2. Whole Numbers: Numbers from 0 (zero) onward are known as Whole numbers, denoted by 'W'.
 $W = \{0, 1, 2, 3, 4, \dots\}$
3. Integers: The collection of all whole numbers and negative of natural numbers are called Integers, denoted by 'Z' or 'I'.
 $Z \text{ or } I = \{\dots, -3, -2, -1, 0, 1, 2, 3, \dots\}$
4. Rational Number: A number which can be expressed as $\frac{p}{q}$ where $q \neq 0$ and $p, q \in Z$ is known as rational number, denoted by 'Q'.
5. Irrational Number: A number which can't be expressed in the form of p/q and its decimal representation is non-terminating and non-repeating is known as irrational number.
e.g., $\sqrt{2}, \sqrt{3}, \pi, \dots 1.732105, \text{ etc.}$
6. The sum of a rational number and an irrational number is always an irrational number.
7. The product of a non-zero rational number and an irrational number is always an irrational number.
e.g., $\frac{2}{3}\sqrt{5}$ is an irrational number.
8. The sum of two irrational numbers is not always an irrational number.
 $(2 + \sqrt{2}) + (2 - \sqrt{2}) = 4$ (a rational number)
9. The product of two irrational numbers is not always an irrational number.
e.g., $(\sqrt{3} - 1)(\sqrt{3} + 1) = 3 - 1 = 2$

Rational numbers

(A) Terminating rational numbers: Remainder becomes 0 after some steps of division in decimal form. For ex- $= 0.25$

(B) Non terminating recurring (repeating) numbers: Remainder never becomes 0 after division in decimal form. For ex- $= 0.333\dots$

Irrational number: Non terminating non recurring. For ex: , ,

Note that square root numbers which are not perfect squares are irrational.
is a perfect sq. of 8, so this is rational.

Some related sums are as follows:

1. Write the following in decimal form and say what kind of decimal expansion each has:

(a) (b)

(a) We have $\frac{36}{100} = 0.36$

$\Rightarrow$ The decimal expansion of $\frac{36}{100}$ is terminating

$$\begin{array}{r}
 0.1818 \\
 11 \overline{) 2.0000} \\
 \underline{-11} \\
 90 \\
 \underline{-88} \\
 20 \\
 \underline{-11} \\
 90 \\
 \underline{-80} \\
 2
 \end{array}$$

(b) Dividing 2 by 11, we have
Here, the repeating block of digits is 18.

$$\Rightarrow \frac{2}{11} = 0.1818\ldots = 0.0\overline{18}$$

Thus, the decimal expansion of $\frac{2}{11}$ is
"non-terminating repeating"

2. Find six rational numbers between 3 and 4.

Ans. We know that there are an infinite number of rational numbers between two rational numbers.

Therefore, six rational numbers between 3 and 4 can be:

Multiply the numbers by

$$3x = < \quad , \quad , \quad , \quad , \quad > 4x =$$

WORKSHEET-2, 2020-21

- Find six rational numbers between 4 and 5.
- Write the following in decimal form and say what kind of decimal expansion each has:
(a) (b)
- Find two rational numbers between and
- Classify the following numbers as rational or irrational:
(i) $\sqrt{23}$ (ii) $\sqrt{225}$
(iii) 0.3796 (iv) 7.478478
(v) 1.101001000100001...
- Classify the following numbers as rational or irrational:
(i) $2 - \sqrt{5}$ (ii) $(3 + \sqrt{23}) + \sqrt{23}$
(iii) $\frac{2\sqrt{7}}{7\sqrt{7}}$ (iv) $\frac{1}{\sqrt{2}}$
(v) 2π
- Simplify each of the following expressions:
(i) $(3 + \sqrt{3})(2 + \sqrt{2})$ (ii) $(3 + \sqrt{3})(3 - \sqrt{3})$
(iii) $(\sqrt{5} + \sqrt{2})^2$
(iv) $(\sqrt{5} - \sqrt{2})(\sqrt{5} + \sqrt{2})$